# Structure of Aquatetrafluorozirconium(IV) 

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#### Abstract

$\left[\mathrm{ZrF}_{4}\left(\mathrm{H}_{2} \mathrm{O}\right)\right], M_{r}=185 \cdot 24$, crystallizes in the tetragonal space group $I \overline{4} 2 d$ with $a=7.724$ (2), $c=$ 11.678 (4) $\AA, Z=8, U=696.7 \AA^{3}, D_{m}=3.500, D_{c}=$ $3.533 \mathrm{Mg} \mathrm{m}^{-3}, \mu($ Mo $K a)=3.068 \mathrm{~mm}^{-1}$. Final $R=$ 0.026 for 414 observed reflexions. The basic structural unit is $\left[\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]$ with dodecahedral coordination. The $\mathrm{Zr}-\mathrm{F}$ distances are 2.058 (2), $2 \cdot 100$ (3) and $2 \cdot 170$ (2) $\AA$ and $\mathrm{Zr}-\mathrm{O}(W)$ is $2 \cdot 132$ (1) $\AA$. Each Zr polyhedron shares six corners with six adjacent polyhedra forming an infinite three-dimensional network.


## Introduction

A mono- and a trihydrate of zirconium tetrafluoride were reported by Chauvenet (1920). In addition to chemical analysis, X-ray powder diffraction (D’Eye, Burden \& Harper, 1956), IR (Kolditz \& Feltz, 1961) and NMR (proton and fluorine magnetic resonance) (Maričić, Strohal \& Veksli, 1963) techniques were used in characterizing these zirconium fluorides. The $\mathrm{ZrF}_{4} /$ $\mathrm{H}_{2} \mathrm{O}$ system has been reinvestigated by Waters (1960). Unit-cell parameters of $\mathrm{ZrF}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ given by Waters (1960) are in good agreement with our data.

## Experimental

The space group was determined from Weissenberg photographs recorded with $\mathrm{Cu} K a$ radiation. The diffraction symmetry and extinctions indicated the space group $I \overline{4} 2 d$ and this was confirmed during
structure refinement. The intensities were collected with a crystal of dimensions $0.020 \times 0.030 \times 0.04 \mathrm{~mm}$ on a Philips PW 1100 computer-controlled four-circle diffractometer in the $\omega$-scan mode [scan width $=$ $1.60^{\circ}(\theta)$, scan speed $=0.040^{\circ}(\theta) \mathrm{s}^{-1}$ ] with graphitemonochromated Mo $K \alpha$ radiation. 414 independent reflexions $[I>2 \sigma(I)]$ in the range $3<\theta<34^{\circ}$ were recorded and used in the calculations. Three standard reflexions were measured every 2 h . The data were corrected for background, Lorentz and polarization effects.

## Structure determination and refinement

The Patterson map was solved in $I \overline{4} 2 d$, which showed that the Zr atom is positioned on the twofold axis at site $8(d)$. A Fourier synthesis based on the coordinates of the Zr atom revealed the two F atoms in general positions and a water molecule on the other twofold axis, site $8(c)$. The structure was refined by full-matrix least squares, minimizing $\sum w\left(\left|F_{o}\right|-\left|F_{c}\right|\right)^{2}$. Weights were assigned as $w=w_{1}, w_{2}$ where $w_{1}=1$ for $\left|F_{o}\right|$ $\leq 35$ and $35 /\left|F_{o}\right|$ for $\left|F_{o}\right|>35 ; w_{2}=1$ for $\sin \theta \geq$ 0.40 and $\sin \theta / 0.40$ for $\sin \theta<0.40$. A scale factor, atomic coordinates, and anisotropic thermal parameters ( 29 variables in all) were refined. Anisotropic thermal parameters are in the usual range: the maximum value is $U_{33}$ for $F(1)$ [0.033 (1) $\left.\AA^{2}\right]$. The final $R=0.026$ and $R_{w}=0.030$ for 414 reflexions with $I>2 \sigma(I)$.

The scattering factors given by Cromer \& Mann (1968) were used. An anomalous-dispersion correction was included for Zr (Cromer \& Liberman, 1970).
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Table 1. Atomic coordinates ( $\times 10^{5}$ ) and equivalent isotropic thermal parameters ( $\times 10^{2}$ ) with e.s.d.'s in parentheses

| $U_{\mathrm{eq}}=\frac{1}{3} \sum_{i} \sum_{j} U_{i j} a_{i}^{*} a_{J}^{*} \mathbf{a}_{i} \cdot \mathbf{a}_{j}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ | $z$ | $U_{\text {eq }}\left(\AA^{2}\right)$ |
| Zr | $10800(5)$ | 25000 | 12500 | $0.52(6)$ |
| $\mathrm{O}(W)$ | 0 | 0 | $15466(28)$ | $0.65(14)$ |
| $\mathrm{F}(1)$ | $29533(41)$ | $11750(38)$ | $22149(30)$ | $2.20(24)$ |
| $\mathrm{F}(2)$ | $22519(31)$ | $42639(31)$ | $24711(22)$ | $1.29(18)$ |

Calculations were carried out on a Univac 1110 computer at the University Computing Centre in Zagreb with the XRAY system (Stewart, Machin, Dickinson, Ammon, Heck \& Flack, 1976). Atomic coordinates and equivalent isotropic thermal parameters are listed in Table 1.*

## Description and discussion of the structure

## Zirconium coordination

The Zr atom is coordinated by six F atoms $[\mathrm{F}(1)$, $\left.F(2), F\left(1^{1}\right), F\left(2^{1}\right), F\left(2^{\text {li }}\right), F\left(2^{\text {III }}\right)\right]$ and two water molecules $\left[\mathrm{O}(W), \mathrm{O}\left(W^{\text {lv }}\right)\right]$ forming $\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ structural units. The polyhedron around the Zr atom is a dodecahedron (Fig. 1) which shares corners with six adjacent polyhedra. The $\mathrm{Zr}-\mathrm{F}$ distances are 2.058 (2), $2 \cdot 100$ (3) and $2 \cdot 170$ (2) $\AA$ and $\mathrm{Zr}-\mathrm{O}(W)$ is $2 \cdot 132$ (1) $\AA$ (Table 2). An analogous structural unit of [ $\left.\mathrm{HfF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]$ is found in the structure of catena-diaqua-di- $\mu$-fluoro-difluorohafnium(IV) monohydrate (Hall, Rickard \& Waters, 1971), one of the dimorphs of $\mathrm{HfF}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$. Here however the overall crystal structure is different.

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Fig. 1. The $\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ dodecahedron compared with an ideal polyhedron.

Table 2. Bond distances $(\AA)$ and angles $\left(^{\circ}\right)$ within the Zr polyhedron

| $\mathrm{Zr}-\mathrm{O}$ | $2 \cdot 132$ (1) | $F(1) \cdots F\left(2^{\text {II }}\right.$ ) | 3.119 (4) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Zr}-\mathrm{F}(1)$ | $2 \cdot 100$ (3) | $F(2) \cdots F\left(2^{\text {II }}\right.$ ) | 2.589 (3) |
| $\mathrm{Zr}-\mathrm{F}$ (2) | $2 \cdot 170$ (2) | $\mathrm{F}\left(2^{\text {iII }}\right) \cdots \mathrm{F}\left(2^{\text {iiII }}\right)$ | 3.011 (4) |
| $\mathrm{Zr}-\mathrm{F}\left(2^{\text {II }}\right.$ ) | 2.058 (2) | $\mathrm{O}(W) \cdots \mathrm{F}(1)$ | 2.576 (3) |
| $F(1) \cdots F\left(1^{\prime}\right)$ | 3.044 (5) | $\mathrm{O}(W) \cdots \mathrm{F}\left(2^{\prime}\right)$ | 2.547 (3) |
| $F(1) \cdots F(2)$ | 2.465 (4) | $\mathrm{O}(W) \cdots \mathrm{F}\left(2^{\text {li }}\right.$ ) | 2.479 (3) |
| $F(1) \cdots F\left(2^{\prime}\right)$ | 2.632 (4) | $\mathrm{O}(W) \cdots \mathrm{F}\left(2^{\text {liII }}\right)$ | 2.595 (3) |
| $\mathrm{F}(1)-\mathrm{Zr}-\mathrm{F}(2)$ | $70 \cdot 5$ (1) | $\mathrm{F}\left(2^{\text {III }}\right)-\mathrm{Zr}-\mathrm{F}\left(2^{\text {IIII }}\right.$ ) | 94.0 (1) |
| $\mathrm{F}(1)-\mathrm{Zr}-\mathrm{F}\left(1^{\prime}\right)$ | 92.9 (1) | $\mathrm{O}(W)-\mathrm{Zr}-\mathrm{F}(1)$ | 75.0 (1) |
| $\mathrm{F}(1)-\mathrm{Zr}-\mathrm{F}\left(2^{\text {II }}\right.$ ) | 97.2 (1) | $\mathrm{O}(W)-\mathrm{Zr}-\mathrm{F}\left(2^{\text {II }}\right.$ ) | 72.5 (1) |
| $\mathrm{F}(2)-\mathrm{Zr}-\mathrm{F}\left(1^{\prime}\right)$ | 76.1 (1) | $\mathrm{O}(W)-\mathrm{Zr}-\mathrm{F}\left(2^{\text {III }}\right.$ ) | 76.5 (1) |
| $\mathrm{F}(2)-\mathrm{Zr}-\mathrm{F}\left(2^{\text {II }}\right.$ ) | 75.5 (1) | $\mathrm{O}(W)-\mathrm{Zr}-\mathrm{F}\left(2^{1}\right)$ | 72.6 (1) |

Symmetry code: (i) $x$, $\frac{1}{2}-y, \frac{1}{4}-z$; (ii) $\frac{1}{2}+y, \frac{1}{2}-x, \frac{1}{2}-z$ : (iii) $\frac{1}{2}+y, x,-\frac{1}{4}+z$; (iv) $-x, \frac{1}{2}+y, \frac{1}{4}-z$.


Fig. 2. View of the crystal structure along a. Each $\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ dodecahedron shares six corners with six adjacent polyhedra forming an infinite three-dimensional network. The atoms connected to the Zr atom with dashed lines are translated +1 in the $\mathbf{x}$ direction.

Table 3. Geometrical parameters for the real dodecahedron compared with the hard-sphere model and most favourable polyhedron (Hoard \& Silverton, 1963) (see Fig. 1)

The unit of length is the mean Zr -ligand distance.

| $\left[\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]$ | Hard-sphere <br> model | Most favourable <br> polyhedron |
| :--- | :--- | :--- |
| $a=1.18$ | $a=m=g=1.199$ | $a=m=1.17$ |
| $m=1.17$ |  |  |
| $g=1.23$ | $b=1.499$ | $b=1.24$ |
| $b=1.48$ | $\theta_{A}=36.9^{\circ}$ | $b=1.49$ |
| $\theta_{A}=36.3^{\circ}$ | $\theta_{A}^{\circ}=35.2^{\circ}$ |  |
| $\theta_{B}=6.9^{\circ}$ | $\theta_{B}^{\circ}=69.5 \circ^{\circ}$ | $\theta_{B}=73.5^{\circ}$ |
| $M-A / M-B=1.03$ | $M-A / M-B=1.00$ | $M-A / M-B=1.03$ |



Fig. 3. The three-dimensional network of polyhedra showing the channels between the $\mathrm{F}(1)$ corners of the polyhedra parallel to a at $\mathbf{b} \simeq 0, \mathbf{c} \simeq \frac{1}{8} ; \mathbf{b} \simeq \frac{1}{2}, \mathbf{c} \simeq \frac{1}{8}$ and parallel to $\mathbf{b}$ at $\mathbf{a} \simeq 0, \mathbf{c} \simeq \frac{1}{8}$; $a \simeq \frac{1}{2} ; \mathbf{c} \simeq \frac{1}{8}$.

Geometrical parameters of the $\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)$ dodecahedron are compared with the hard-sphere model (Hoard \& Silverton, 1963; Kepert, 1965, 1978) in Table 3. The shape of the dodecahedron is defined by the angles $\theta_{A}, \theta_{B}$ made by the bonds $M-A, M-B$ with the unique axis and the ratio of the bond lengths. The occurrence of an infinite network of polyhedra instead of discrete polyhedra, and dissimilar ligands $[\mathrm{F}, \mathrm{O}(W)]$ together with the ligand repulsions cause the departure of the dodecahedron from ideality. A more stable structure can often be obtained by distortion of the structure based on the hard-sphere model and this is observed here.

## Molecular packing

The structure consists of a three-dimensional network of $\mathrm{ZrF}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}$ polyhedra sharing six corners (Fig. 2) through atoms $\mathrm{O}(W), \mathrm{O}\left(W^{\text {lv }}\right)$, and $\mathrm{F}(2), \mathrm{F}\left(2^{1}\right)$, $F\left(2^{\text {II }}\right), F\left(2^{\text {III }}\right) . F(1)$ and $F\left(1^{\prime}\right)$ are disposed at free corners of the polyhedron. Fig. 3 shows the threedimensional network of polyhedra. The water molecule is surrounded by eight F atoms arranged at the corners of a cube at distances $\mathrm{O}(W) \cdots \mathrm{F} 2.479$ (3), 2.547 (3), 2.576 (3) and 2.595 (3) A. A trifurcated $\mathrm{O}(W)-\mathrm{H} \cdots \mathrm{F}$ hydrogen bond might be expected.

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# Neutron Powder Diffraction Investigation of Pure and Deuterated Palladium Phosphide $\mathbf{P d}_{6} \mathbf{P}$ 

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#### Abstract

A structure proposal for $\mathrm{Pd}_{6} \mathrm{P}$ has been refined by the Rietveld method from neutron powder diffraction 0567-7408/81/111965-08\$01.00 profile data to a weighted profile $R_{w p}$ value of 0.055 , based on 1000 measured points in the profile. The space group is $P 2_{1} / c$ with $a=5.6740(4), b=$ 9.4409 (6), $c=8.2100$ (6) $\AA$, $\beta=110.414$ (4) ${ }^{\circ}, U=$ c 1981 International Union of Crystallography


[^0]:    * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 36140 ( 9 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

